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by Maurice L. Hartung
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THIS IS THE FIRST BOOK OF THE BASIC MATHEMATICS PROGRAM, WHICH IS A UNIT OF THE CURRICULUM FOUNDATION SERIES.
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UNDER THE DIRECTION OF GEORGE E. RUSSELL, DIRECTING EDITOR OF THE BASIC MATHEMATICS PROGRAM.
THIS BOOK WAS DESIGNED BY WILLIAM NICOLL AND ILLUSTRATED BY JULIA KOLB.
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## Purpose and Scope of This Book

Numbers We See is designed to help teachers develap a rich and interesting number-readiness pragram in Grade 1. Used either with the Number Readiness Chart, ${ }^{1}$ the Arithmetic Readiness Cards, ${ }^{2}$ Our Number Warkshap $1,{ }^{3}$ ar independently, it leads to a systematic develapment of number cancepts by nan-farmal, concrete methads. Carefully planned pictures are used ta intraduce each new cancept in a natural setting at the child's level of interest and understanding. The number ideas in each picture can be made clear through graup discussian and a variety af manipulative activities based an the picture. Detailed plans far using the baak and many suggested activities will be faund in the Teacher's Edition beginning an page 73. Numbers We See develops five basic phases af number readiness. 1 Carrespandence: relating ane object ta ane abject, ane-ta-twa, twa-to-ane, ane-ta-ten, recagnizing graups af twa, three, and faur abjects. (Pages devated ta this phase are indicated by blue blacks in the baak.)
2 Number relatianships: finding how graups af abjects (up ta ten) can be built up fram the small groups and haw these larger graups can be braken up inta variaus arrangements af the smaller graups. (Indicated by red.)
3 Number system: grauping by tens as well as by tens in cambinatian with anes, leading up ta an appreciation af the written natatian of our number system. (Indicated by arange.)
4 Measurement: develaping the cancept af a unit and standard unit; counting the number of times the unit is used. (Indicated by green.)

Maney: recagnizing the smaller coins; knawing the relatianships between them and what they will buy. (Indicated by gray.)

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## Concept Chart

## Concepts and Skills

This poge introduces the family and the book to the children.

Informal reactions to quantitative ideas of mony and few without counting Reoctions to quantitotive ideas of many and few in simple comparisons
Simple pairing; motching one series of objects to onother; continued on page 7 Simple pairing; emphasis on ideas of enough, not enough, all
Simple poiring; emphosis on ideas of too few, too many, more than enough Simple pairing; emphasis on ideas of as mony as, not as mony as, more, fewer Informal reoctions to standards that arise from use or need
Immediote recognition of model groups of two and three
Differentiating between groups of two and three objects
Active groupings by two and three occording to position and other choracteristics Recognition of groups of four and differentioting between two and four Differentiating between right and wrong with respect to groups of two and three Positionol meoning of eoch of the numbers 1 to 5 ; emphosis on 1,3 and 5 Positional meaning of 1 to 5 ; emphosis on 2 and 4 ; recognition of symbols 1 to 5 Positional meoning of 1 to 5; emphasis on location in two directions

Positional meoning of 1 to 5 ; recognition of groups of two, three, and four
Formation of 6 by adding a group of 2 to 2,2 , or $4 ; 6$ as 3,$3 ; 6$ os $2,2,2$

Formation of 8 by adding o group of 2
to o group of $6 ; 8$ as 4,$4 ; 8$ os $2,2,2,2$
Formotion of 10 by odding a group of 2 to a group of $8 ; 10$ os 5,$5 ; 10$ as $2,2,2,2,2$

## Picture Sequence

Father, Mother, Carol, Don, and Noncy at home in their living room
Night scene showing the community in which the family lives
Scenes from the neighborhood in which the fomily lives
The street on which the fomily lives, showing its house ond four others
Continuotion of page 6

Corol hos a porty including herself and four of her friends.
Corol and her mother straighten up the house after the party.
The fomily picks opples from the tree in the back yord.
Toys and objects that are familiar to the children
Don ploys marbles with one of his friends.
Carol and Don with friends at the ployground
The family watches the circus parade.

A scene from the circus which the family ottends
The children buy fickets for the troin ride at the circus.
The children board the train.
Baggage rock for checking children's toys during train rides
Toys belonging to Corol, Don, Nancy, and their friends
Don and Carol with friends at the school ployground
Corol plays o game with friends of school.
Lunch time at school

Concepts and Skills
Recognition of groups that make up group: of 6,8 , and 10 ; combining; separating Formation of 5 by assembling 2 's and 1 extra; 5 as $2,2,1$; as 3,2 ; as 4,1
Formation of 7 by assembling 2 's and 1 extra; 7 as $2,2,2,1$; as $3,3,1$; as 6,1 Formation of 9 by assembling 2 's and 1 extra; 9 as $2,2,2,2,1$; as $4,4,1$; as 8,1 Recognition of $5,6,7,8,9$, and 10 by groupings previously developed
The unit in measurement; using measuring model once for each object
Using more than one copy of a measuring model to measure each object
Using one measuring model repeatedly in situations that measure exactly
Using one measuring model repearedly in situations that do not measure exactly Positional meaning of 6 to 10 ; recognition of number symbols 6 to 10
Positional meaning of 6 to 10 ; emphasis on location in two directions
Positional meaning of 6,210 ; review of measurement and simple pairing
Distributing 1 thing to 2 things; 1 -to-2 correspondence
Rearranging groups of 6 as $2,2,2$ by partial combining; 6 as 4,$2 ; 6$ as 2,4 Rearranging groups of 8 as $2,2,2,2$ by partial combining; 8 as 6,$2 ; 2,6 ; 4,4$
Rearranging groups of 10 as $2,2,2,2,2$
10 as 8,2 ; as 2,8 ; as 6,4 ; as 4,6
Recognition of 6,8 , and 10 as made up of arrangements of groups of 2
Using more than one copy of a measuring model to measure volume or capacity

Using one measuring model repeatedly to measure volume or capacity
Meaning of 6 as made up of the groups $1,2,3$ and combined to 3,$3 ; 4,2 ; 5,1$ Assembling the correct component groups to make 6
Meaning of 7 as made up of the groups 2,3,2 and combined to 4,$3 ; 5,2$
Assembling the correct component groups to make 7, including 6,1
Recognition of 6 and 7 by their component groups

## Picfure Sequence

Toy automobiles belonging to the children
Don and his friends play a game of "hide and seek."
Don and his friends have a "wheelbarrow" race.
Don and his friends have a "relay" race.

Toys and objects familiar to the children

Don takes part in a measuring activity at school.
Don and his classmates use measurement in planning a blackboard decoration.
Don measures off the distance for a game of ring toss.
Don, Carol, and two friends play beanbag.
Scene from the children's pet show at school
Parents gather for the pet show.

Carol, Don, Nancy, and a friend at play
Toy shop at which the children buy their toys
The children visit the farm. Carol feeds her pet chickens.
The children visit the farm. Don helps ake care of the cows.
The children visit the farm. Carol and Nancy watch the ducks.
Arrangements of ducks and chickens

Carol and Don pick berries at the farm.
Continuation of page 40
The children watch a puppet show at a school program.
Animals and objects used in the puppet show
The children perform at the school program.
Animals imitated by children in their performances at the school program Dances and arrangements suggested by the school program

Recognition of 9 by adding a group of 3 to two groups of $3 ; 9$ as 6,$3 ; 9$ as $3,3,3$ Meaning of 8 as made up of the groups 2,3,3 and combined to 6,$2 ; 5,3$ Assembling the correct component groups to make 8 , including 4,$4 ; 7,1$
Meaning of 9 as made up of the groups $2,3,4$ and combined to 5,$4 ; 6,3 ; 7,2$ Assembling the correct component groups to make 9 , including 8,1
Meaning of 10 as made up of the groups $1,2,3,4 ; 10$ as 2,$8 ; 4,6 ; 5,5 ; 3,7 ; 9,1$ Assembling the correct component groups to make 10
Recognition of $6,7,8$, and 9 by their component groups
Recognition of 8,9 , and 10 by their component groups
Establishing decades by counting with emphasis on decade names; 20, 30 Establishing decades by counting with emphasis on decade names ; 40, 50 Establishing decades by counting with emphasis on decade names; 60, 70, 80 Establishing decades by counting with emphasis on decade names; 90, 100 Meaning of numbers within the decades; distinguishing between tens and ones Meaning of numbers within the decades; distinguishing between tens and ones Naming and writing numbers from 11 to 100; emphasis on tens and ones
Naming and writing numbers from 11 to 100; emphasis on tens and ones Establishing relationship between 10 cents and 1 dime
Establishing relationship between 5 cents and 1 nickel; 2 nickels and 1 dime Identifying correct amounts of money to purchase items with prices indicated Reacting to crude meosurements and positional meaning of 1 to 10; inventory Recognition of the numbers 3 to 10 by their component groups; inventory Recagnition of the numbers 3 to 10 by their component groups; inventory
Applying concept of a standard in measurement; inventory

## Picture Sequence

The band at the school program
Don and his friends at play. They race with their tricycles.
Toys belonging to Don and his friends
Don and his friends at play. They have a boat race.
Arrangements suggested by the boat race
Don and his friends at play. They fly their kites.
Arrangements suggested by the kites
Toys of interest to the children

Toys of interest to the children

Don builds a village of $\log$ houses with toy logs.
Continuation of page 56

Continuation of page 57
Continuation of page 58

Don ond a friend lay out logs for more houses.
Continuation of page 60

Carol and a friend have a play store.
Continuation of page 62

Carol and Don buy candy for themselves and their friends.
Carol, Don, and their friends buy icecream cones.
Things that interested Carol and Don when they went to the store
Toys and pets of interest to the children
Toys and pets of interest to the children

## Continuation of page 68

Items of interest to children at home and at school

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[^0]:    1 Number Readiness Chart, by Anita Riess and Maurice L. Hartung. Scatt, Faresman and Campany.
    2 Arithmetic Readiness Cards Set 1: Grauping; Set 2: Number System, by Maurice L. Hartung, Henry Van Engen, and Helen Palmer. Scatt, Faresman and Campany.
    3 Our Number Warkshap 1, by Maurice L. Hartung, Henry Van Engen, and Catharine Mahaney. Scatt, Faresman and Campany.

